

# Biometric Classifier Update using Online Learning: A Case Study in Near Infrared Face Verification

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## Abstract

The performance of large-scale biometric system deteriorates over time as new individuals are continually enrolled. To maintain a high level of performance, the classifier has to be re-trained offline in batch mode using both the existing and new data. The process of re-training can be computationally expensive and time consuming. This paper presents a new biometric classifier update algorithm that incrementally re-trains the classifier using online learning and progressively establishes a decision hyperplane for improved classification. The proposed algorithm incorporates soft labels and granular computing in the formulation of  $2\nu$ -Online Granular Soft Support Vector Machine to re-train the classifier using only the new data. Granular computing makes it adaptive to local and global variations in data distribution, while soft labels provide resilience to noise. Each time a data is acquired, new support vectors that are linearly independent are added and existing support vectors that do not improve the classifier performance are removed. This constrains the size of the support vectors and significantly reduces the training time without compromising the classification accuracy. The efficacy of the proposed online learning strategy is validated in a near-infrared face verification application involving different covariates. The results obtained on a heterogeneous near-infrared face database of 328 subjects show that in all experiments using different feature extraction and classification algorithms the proposed online  $2\nu$ -Granular Soft Support Vector Machine learning approach is 2-3 times faster while achieving a high level of accuracy similar to offline training using all data.

## *Key words:*

Biometrics, Online learning, Support vector machine, Near infrared face verification

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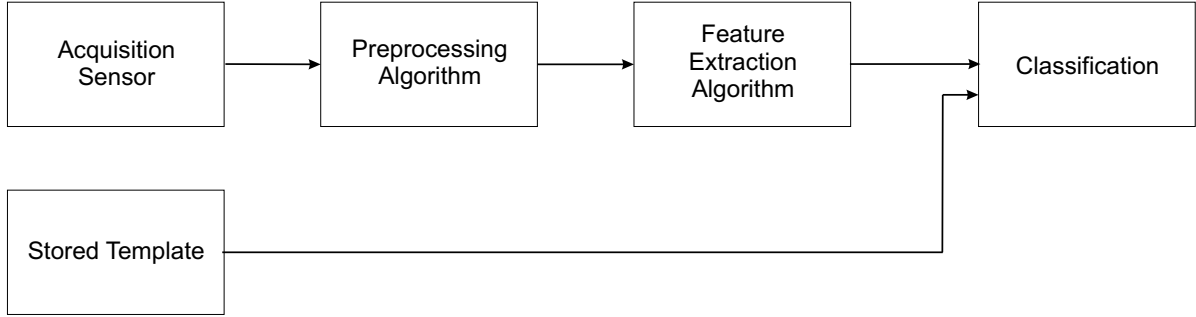


Fig. 1. Block diagram representing the modules of a biometric system that may require regular update or re-training.

## 1 Introduction

A carefully designed biometric system should be stable and robust to environmental dynamics and variations in the data distribution. However, in real world applications, these systems are affected by several factors including template aging, improper interaction of the user with the sensor, and noise. Furthermore, as the size of a biometric database increases, the system has to re-train itself in order to handle the variations introduced due to the newly enrolled subjects. For example, an identification system may have to re-compute its thresholds to handle the increased number of subjects, a verification system may have to re-compute its decision boundaries based on the new set of genuine and impostor scores, and a face verification system may have to update its templates to address the aging effects of the face biometric. The re-training process can be time consuming and may not be pragmatic in large scale applications. A generic biometric system, as shown in Fig. 1, has five modules that require regular update or re-training. Template update is required to address the issue of template aging, sensor update is necessary to accommodate advancements in sensor technology, re-training of the preprocessing and feature extraction algorithms is necessary to handle variations in data, and classifiers have to be updated to account for changes in the intra-class and inter-class dynamics of the subjects.

The paper focuses on developing online learning algorithm at the classifier level when the number of subjects is increased. Currently, biometric classifiers such as support vector machine (SVM) and neural network are trained *offline* with the available training data and domain specific knowledge. However, large scale biometric applications such as US-VISIT and FBI-IAFIS continuously enroll new individuals. Due to the high computational complexity required for re-training in such applications, it is not feasible to regularly update the classifier knowledge and decision boundary, thereby affecting the verification performance of the biometric system. Online learning presents an efficient alternative to offline learning and classification by updating the classifier knowledge upon the arrival of new data. While it has been extensively

used in problems related to machine learning [1]-[7], *online learning is not very well exposed in biometrics*, though some of the existing online learning algorithms show experimental results on face recognition [6], [7]. Existing research present incremental learning for face recognition algorithms such as principle component analysis and linear discriminant analysis and results have shown the usefulness of incremental algorithms. Considering the high applicability of this concept in biometrics, this paper presents the concept of online learning for biometric classifier training and update.

The contribution of the research lies in incorporating soft labels [9] and granular computing in the formulation of  $2\nu$ -Support Vector Machine ( $2\nu$ -SVM) [10] to design a  $2\nu$ -Granular Soft Support Vector Machine ( $2\nu$ -GSSVM) and applying the online learning concept for classifier update. The introduction of soft labels and granular computing increases the classification performance while online learning enables the classifier to update its knowledge as database enrollment increases. The performance of the algorithm is evaluated in the context of a *near infra-red (NIR) face verification application*. Facial features are computed using Principal Component Analysis (PCA) [11], Linear Discriminant Analysis (LDA) [12] and modified C2 features [13]. Experiments performed on a heterogeneous NIR face database indicate that the proposed online learning based classification algorithm not only improves the accuracy but also reduces the training time significantly.

## 2 Why Online Learning is Applicable in Biometrics?

Online learning is a concept from machine learning and inspired by human cognition. Humans are very good in adapting to the environment and learning concepts based on new information. Starting from childhood, a natural learning process constantly trains the human mind to develop new abilities and sustain old (useful) behavior. It also learns to remove behaviors or patterns that become extraneous and redundant over time. Thus, online learning has two components namely incremental and decremental learning.

Mathematically, we have the instance space  $I$  consisting of patterns, label space  $Y$  indicating the classes of patterns, and a learning based classifier  $\mathfrak{S}$ . The task of the classifier  $\mathfrak{S}$  is to map  $I$  to  $Y$  using training examples. In general, there are two modes of learning: (1) offline/batch learning mode and (2) online learning mode. In batch mode, a set of training samples  $(x_i, y_i) \in I \times Y$  ( $i = 1, \dots, N$  and  $N$  is number of training samples) are used as input. The learning classifier,  $\mathfrak{S}_B$  ( $B$  denotes batch mode), attempts to obtain a robust/optimal solution such that  $\mathfrak{S}_B(x_i) = y_i$ . Unlike batch learning, in the online learning mode, training samples become available in a sequential manner. In other words, at time  $j$ , training sample  $(x_j, y_j)$  and previously processed

samples  $(x_1, y_1), \dots, (x_{j-1}, y_{j-1})$  are used to train the learning classifier  $\mathfrak{S}_O$  ( $O$  denotes online mode) by predicting  $y'_j = \mathfrak{S}_O(x_j)$  and comparing it with the true label  $y_j$ . The objective of online learning classifier is to accommodate new training samples and minimize the error over the whole training sequence. It is intuitive that online learning is pertinent to real world biometric applications where training samples are available sequentially (one at a time) and data representation must be updated for optimal classification performance. Another important aspect of online learning is that for a large scale application, it is computationally efficient to solve the offline/batch training process in an online manner [2].

In large scale real world biometrics applications, it is challenging and computationally complex to train a classifier in advance. Without re-training, the disparate characteristics of additional biometric data can cause the performance to degrade. However, training the classifier dynamically online facilitates updated learning in real-time by reducing the computational cost. In a typical biometric system, online learning can be applied to any module that requires training and learning. *In this paper, we propose a  $2\nu$ -Online Granular Soft Support Vector Machine ( $2\nu$ -OGSSVM) and apply it in the classification stage of the biometric system.*

### 3 Formulation of $2\nu$ -Online Granular Soft Support Vector Machine

In general, an SVM is used for binary classification problems. Let  $\{\mathbf{x}_i, y_i\}$  be the set of  $N$  data vectors where  $i = 1, \dots, N$ ,  $\mathbf{x}_i \in \mathfrak{R}^d$  and  $y_i$  is the hard label such that  $y_i \in (+1, -1)$ . The basic principle of SVM is to find the hyperplane that separates the two classes with the widest margin, i.e.,  $\mathbf{w}\varphi(\mathbf{x}) + b = 0$  to minimize,

$$\begin{aligned} & \frac{1}{2}\|\mathbf{w}\|^2 + C \sum_i \psi_i \\ & \text{subject to } y_i (\mathbf{w} \varphi(\mathbf{x}_i) + b) \geq (1 - \psi_i), \quad \psi_i \geq 0 \end{aligned} \tag{1}$$

where  $b$  is the offset of the decision hyperplane,  $\mathbf{w}$  is the normal weight vector,  $\varphi(\mathbf{x})$  is the mapping function used to map the data space to the feature space and provide generalization for the decision function.  $C$  is the regularization factor between the total distance of each error from the margin and the width of the margin, and  $\psi_i$  is the slack variable used for classification errors [14]. The optimal SVM parameters are obtained by manually setting the parameters until an optimal error rate is achieved. This heuristic process is very time consuming. Dual  $\nu$ -SVM ( $2\nu$ -SVM), originally proposed by [10], is a computationally efficient variant of SVM. It is more flexible in the training

and overcomes the issues when the training class sizes are not same. In Equation 1, additional class dependent parameters ( $\rho$ ,  $\nu$  and  $C_i$ ) are introduced such that the formulation becomes,

$$\begin{aligned} & \min\left\{\frac{1}{2}\|\mathbf{w}\|^2 - \sum_i C_i(\nu\rho - \psi_i)\right\} \\ & \text{subject to } y_i(\mathbf{w} \varphi(\mathbf{x}_i) + b) \geq (\rho - \psi_i), \quad \rho, \psi_i \geq 0 \end{aligned} \quad (2)$$

where  $\rho$  is the position of the margin and  $\nu$  is the error parameter that can be calculated using  $\nu_+$  and  $\nu_-$  which are the error parameters for training the positive and negative classes respectively.

$$\nu = \frac{2\nu_+\nu_-}{\nu_+ + \nu_-}, \quad 0 < \nu_+ < 1 \quad \text{and} \quad 0 < \nu_- < 1 \quad (3)$$

$C_i(\nu\rho - \psi_i)$  is the cost of errors and  $C_i$  is the error penalty for each class which is calculated as,

$$C_i = \begin{cases} C_+, & \text{if } y_i = +1 \\ C_-, & \text{if } y_i = -1 \end{cases} \quad (4)$$

where,

$$C_+ = \frac{\nu}{2n_+ + \nu_+}, \quad (5)$$

$$C_- = \frac{\nu}{2n_- + \nu_-}.$$

Here,  $n_+$  and  $n_-$  are the number of training points for the positive and negative classes respectively. Further, the  $2\nu$ -SVM objective function can be formulated as (Wolfe Dual formulation),

$$L = \sum_i \alpha_i - \left\{ \frac{1}{2} \sum_{i,j} \alpha_i \alpha_j y_i y_j K(x_i, x_j) \right\} \quad (6)$$

where  $i, j \in 1, \dots, N$ ,  $K(\mathbf{x}_i, \mathbf{x}_j)$  is the kernel function [14],  $\alpha_i, \alpha_j$  are the Lagrange multipliers such that  $0 \leq \alpha_i \leq C_i$ ,  $\sum_i \alpha_i y_i = 0$ , and  $\sum_i \alpha_i \geq \nu$ .

During training, it is possible that some of the data points may be noisy or incorrectly labeled. In such cases, like any classifier,  $2\nu$ -SVM performs erroneous classification. To address this limitation, the formulation of  $2\nu$ -SVM is extended to include soft labels [9]. Tao *et al.* have shown that the use of soft

labels not only reduces the classification error but also decreases the number of stored support vectors. Let  $z_i$  be the soft label for the  $i^{th}$  training data  $x_i$ .  $2\nu$ -SVM is transformed into  $2\nu$ -Soft SVM ( $2\nu$ -SSVM) as follows,

$$\begin{aligned} & \min \left\{ \frac{1}{2} \|\mathbf{w}\|^2 - \sum_i C_i (\nu\rho - \psi_i) \right\} \\ & \text{subject to } z_i (\mathbf{w} \varphi(\mathbf{x}_i) + b) \geq z_i^2 (\rho - \psi_i). \end{aligned} \quad (7)$$

Even with  $2\nu$ -SSVM, training a large database is still time consuming. Granular computing [15] is based on divide and conquer approach and is aimed at reducing the computational time as well as increasing the adaptability to data distribution both locally and globally. In the proposed  $2\nu$ -Granular SSVM, the data space is divided into  $c$  subspaces with one  $2\nu$ -SSVM operating on each subspace. This subspace division is performed using standard fuzzy C-means clustering that generates clusters of similar patterns. Let  $2\nu$ -SSVM $_i$  represent the  $i^{th}$   $2\nu$ -SSVM, and  $2\nu$ SSVM $_i : \rightarrow L_i$  represent the  $2\nu$ -SSVM operating on the  $i^{th}$  subspace ( $i = 1, 2, \dots, c$ ). The compound margin width  $W$  is computed using (8).

$$W = \left| \sum_{i=1}^c \frac{t_i}{t} (2\nu SSVM_i : \rightarrow L_i) - L_0 \right|, \quad (8)$$

$$t = \sum_{i=1}^c t_i$$

where  $t_i$  is the number of training data in the  $i^{th}$  subspace.  $2\nu$ -SSVM learning yields  $L_i$  at the local level and  $L_0$  is obtained by learning another  $2\nu$ -SSVM on the complete feature space at the global level. Equation 8 provides the margin width associated with the  $2\nu$ -GSSVM hyperplane.

### 3.1 $2\nu$ -Online GSSVM

Support Vector Machines, including the proposed  $2\nu$ -GSSVM, are trained using a training database and evaluation is performed using a testing database. Several applications including biometrics, that use SVM as a classifier, require re-training at regular intervals to accommodate the changes in data distribution. Re-training the SVM every time is computationally expensive and may not be feasible for real time applications. In this paper, we propose an on-line learning scheme for  $2\nu$ -GSSVM and is termed as  $2\nu$ -OGSSVM. The main concept behind the proposed approach is to first construct the decision hyperplane using an initial training dataset and then re-train the classifier by incorporating the new training data points into the decision hyperplane. It also

removes unnecessary and irrelevant data so that the number of support vectors does not increase drastically with the increase in training samples. *Thus, the proposed online learning algorithm includes both incremental and decremental learning.* In this process, the Karush-Kuhn Tucker conditions [16] are maintained so that the  $2\nu$ -OGSSVM provides an optimal decision hyperplane. The training procedure of  $2\nu$ -OGSSVM is as follows:

- (1)  $2\nu$ -GSSVM is trained using an initial training database and a decision hyperplane is obtained with  $m$  numbers of support vectors.
- (2) For each new training data  $\bar{x}_i$ ,
  - (a)  $\bar{x}_i$  is classified using the trained  $2\nu$ -GSSVM.
  - (b) The classification output is compared with the associated label  $\bar{z}_i$ ; if the classification is correct then re-training is not required.
  - (c) Otherwise,
    - (i) The decision hyperplane is recomputed using the  $m$  trained support vectors and  $\{\bar{x}_i, \bar{z}_i\}$  using standard batch training model<sup>1</sup>.
    - (ii) After recomputing the hyperplane, the number of support vectors increases. If the number of support vectors is more than  $m + \lambda$ , where  $\lambda$  is a threshold that controls number of support vectors, then a support vector that is farthest from the current decision hyperplane is selected.
    - (iii) The selected support vector is removed from the list of support vectors and stored in the list,  $l$ . The classifier with  $m + \lambda - 1$  support vectors is used for validation and testing.
- (3) The support vectors in the list  $l$  are used to test the new classifier. If there is any misclassification, Step 2(c) is repeated to minimize the classification error.
- (4) The least recently included support vectors are removed from the list,  $l$ , in the final classifier.

It is worthwhile noting that for some cases, it may be required to have an exit condition at Step 3 to avoid any deadlock. One possible exit condition can be to include the sample as support vector that is causing deadlock. However, in our case study we have not encountered any deadlock. Fig. 2 shows an example of the decision boundary generated using the proposed  $2\nu$ -OGSSVM approach. The two classes in the example represent the genuine and impostor match scores obtained from a face verification algorithm. Fig. 2a shows the result with 200 training samples. In this case, the  $2\nu$ -SVM uses all 200 training samples as input for off-line or batch learning, while the proposed  $2\nu$ -OGSSVM uses the 200 training samples to perform the initial training for online learning. Fig. 2b compares the performance when the number of training samples is increased

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<sup>1</sup> Number of samples in this recalculation is small and hence computational time is relatively less compared to computing hyperplane with combined old and new training data.

to 400. In this case, the  $2\nu$ -SVM uses all 400 training samples for off-line or batch learning, while the  $2\nu$ -OGSSVM updates the previously trained classifier one sample at a time with the remaining 200 samples for online learning. The figure shows that the proposed  $2\nu$ -OGSSVM efficiently performs binary classification.

#### 4 Application of the Proposed $2\nu$ -OGSSVM to Near Infrared Face Verification

Face verification is a long standing problem in computer vision and researchers have proposed several algorithms to address the challenges of pose, expression and illumination [17]-[19]. Recent studies have shown the usefulness of near infrared face images for verification [20], [21]. Previous research results also suggest that the performance of face verification with NIR images is better than visible spectrum images [21]. This is because, as shown in Fig. 3, the near infrared spectrum, generally, provides resilience to varying image quality, changes in illumination, and minor variations in expression. Therefore, in this case study, NIR face verification is used to evaluate the performance of the proposed  $2\nu$ -OGSSVM classifier.

Fig. 4 shows the steps involved in NIR face verification. Since the proposed  $2\nu$ -OGSSVM is a binary classifier, it can be used for biometric verification. Firstly, the classifier is trained for binary classification (genuine and impostor). Next, at the probe level, facial features are extracted from the NIR face image using feature extraction algorithms (PCA/LDA/C2). Match scores are computed using the Mahalanobis distance measure by comparing the extracted features against the stored features. Finally, classification is performed using the trained classifier.

##### 4.1 Training $2\nu$ -OGSSVM

Let the input training data be  $\{\mathbf{x}_i, z_i\}$  where  $i = 1, \dots, N$ .  $N$  is the total number of training samples and  $\mathbf{x}_i$  is the  $i^{th}$  match score.  $z_i$  is the soft class label and labeling is performed using the density estimation approach [22] similar to Tao *et. al* method [9]. For the  $i^{th}$  training sample, likelihood ratio  $P_i = \frac{g_{gen}(x_i)}{g_{imp}(x_i)}$  is computed where  $g_{gen}$  and  $g_{imp}$  represent the marginal densities of genuine and impostor respectively. If  $P \geq \epsilon$  (where  $\epsilon$  is a very small value and samples belong to the genuine users if the condition holds) then the value of ‘ $P$ ’ is assigned to the soft label along with a ‘+’ sign otherwise, soft label equal to the value of ‘ $P$ ’ with a ‘-’ sign denotes impostor sample.  $2\nu$ -OGSSVM is trained using the radial basis function (RBF) kernel ( $= \exp(-\gamma\|\mathbf{x}_i - \mathbf{x}_j\|^2)$ ).



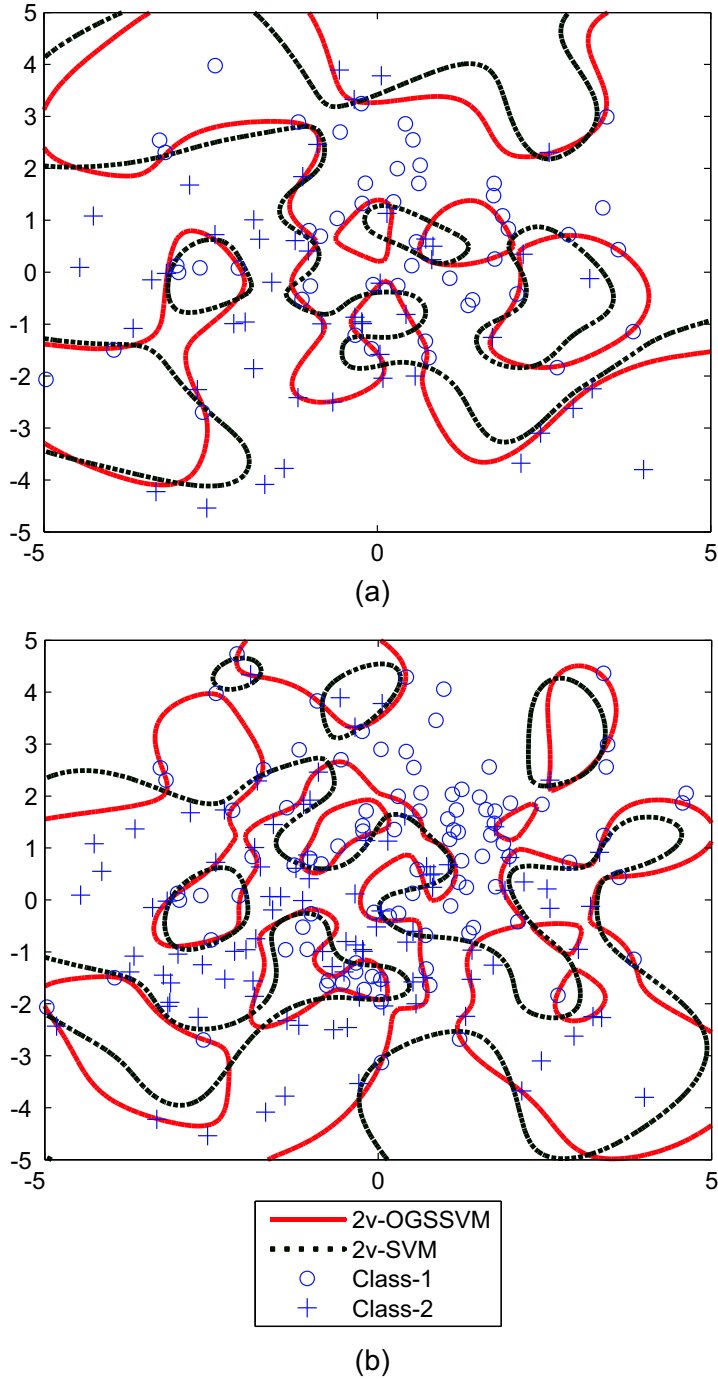


Fig. 2. Comparison of non-linear decision boundary generated with offline learning using  $2\nu$ -SVM and online learning using the proposed  $2\nu$ -OGSSVM. (a) No. of training samples = 200 (b) No. of training samples = 400.

The output of the trained  $2\nu$ -OGSSVM is a non-linear decision hyperplane that can classify genuine and impostor match scores.

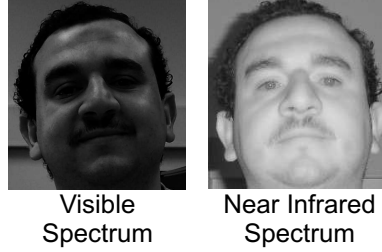


Fig. 3. Visible spectrum and NIR spectrum face images of the same individual under same illumination conditions.

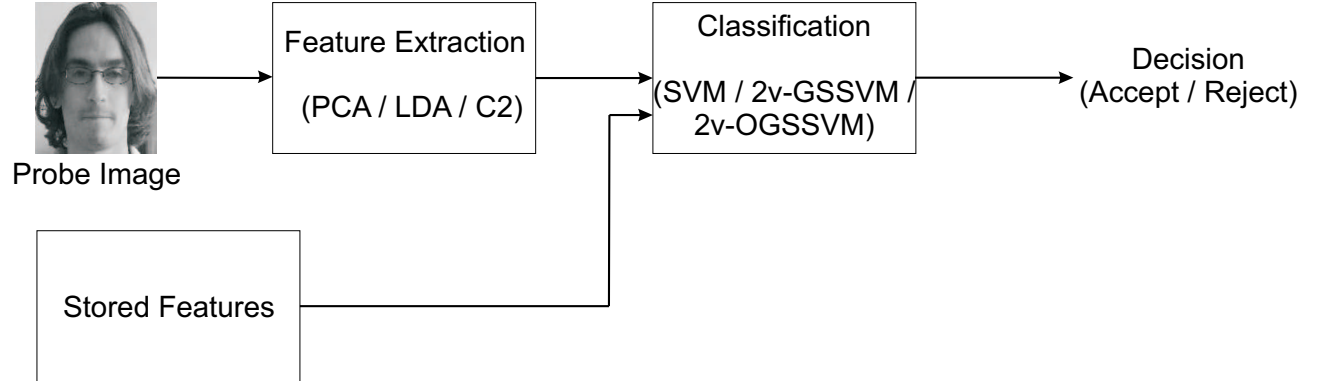


Fig. 4. Illustrating the steps involved in the NIR face verification case study.

#### 4.2 Probe Classification and Decision Making

At the probe level, the trained  $2\nu$ -OGSSVM is used to classify the match scores. The match score obtained by matching the probe and gallery facial features,  $x_p$ , is provided as input to the mixture model and the likelihood ratio  $P_p = \frac{g_{gen}(x_p)}{g_{imp}(x_p)}$  is computed. Finally, the trained  $2\nu$ -OGSSVM is used for classifying the likelihood ratio and a decision of accept or reject is made.

#### 4.3 Experimental Protocol

The images from three NIR face databases are combined to create a relatively large database with heterogeneous characteristics. As shown in Table 1, the CBSR NIR face database contains 3940 images pertaining to 197 subjects, the WVU database [13] contains 560 images belonging to 40 subjects, and the Equinox database has 1307 images from 91 subjects. Fig. 5 shows sample NIR face images from WVU database. The CBSR and Equinox databases contain images that are captured under varying illumination and expression whereas the WVU database contains images with variations in pose, illumination and minor expression. Combining these databases provides a wide range of interclass and intraclass variations that typically occur in real world face

Table 1

Composition of the heterogeneous NIR face database.

Face Database	Number of Subjects	Number of Images per Subject	Number of Images
CBSR	197	20	3940
Equinox	91	8 - 16	1307
WVU	40	14	560
<b>Total</b>	<b>328</b>	–	<b>5807</b>



Fig. 5. Sample NIR face images from the WVU database [13].

verification applications. Size of images in these databases vary significantly, therefore, we detect face images using OpenCV face detector and normalize the detected face images at the size of  $320 \times 240$ . The database is divided into training database and testing database. The training database contains four images of each individual, i.e. total 1312 images, and the remaining 4495 images are used as the testing or probe dataset.

For feature extraction and evaluation, three different algorithms are used. The first facial feature extraction algorithm is the appearance based PCA algorithm [11] and the second algorithm is LDA algorithm [12]. Third algorithm is the modified C2 feature extraction algorithm [13] which is a local texture feature based approach. This algorithm uses 2D log-polar Gabor features and visual cortex model to extract facial features. The training database is used to train these feature extraction algorithms and verification is performed using a two-class classifier such as SVM,  $2\nu$ -GSSVM and  $2\nu$ -OGSSVM. To evaluate the efficacy of the proposed approach, the experimental comparison of SVM,  $2\nu$ -SVM, and  $2\nu$ -GSSVM with online classification ( $2\nu$ -OGSSVM) is performed. For SVM,  $2\nu$ -SVM, and  $2\nu$ -GSSVM, the complete training database is used to train the classifier (batch learning mode). On the other hand, to evaluate the performance of the proposed  $2\nu$ -OGSSVM classifier, it is initially trained with 100 subjects and then online learning is performed with training samples from the remaining 228 subjects i.e., online training with one sample at a time. Further, the train-test partitioning is performed 20 times for cross-validation and ROC curves are generated by computing the false reject rate (FRR) over these trials at different false accept rates (FAR). Finally, verification accuracies are reported at 0.01% FAR.

#### 4.4 Experimental Results

In all the experiments, RBF kernel with  $\gamma = 6$  was used for SVM,  $2\nu$ -SVM,  $2\nu$ -GSSVM and  $2\nu$ -OGSSVM classifiers<sup>2</sup>. In the first case, dimensionality of PCA subspace and PCA coefficients were extracted using standard approach as described in [12] and matching was performed using the Mahalanobis distance measure. The match score was further classified using these classifiers separately. The verification performance of PCA with non-linear classification was also compared with the traditional PCA algorithm [11] (that uses Euclidean distance and a linear decision threshold for classification) and incremental PCA (IPCA) algorithm [6]. This experiment provides the baseline performance to facilitate systematic comparison with other algorithms. Furthermore, accuracies were also computed when IPCA was combined with the proposed  $2\nu$ -OGSSVM (i.e. IPCA +  $2\nu$ -OGSSVM, both feature extraction and classification algorithms were online). Similar to the PCA experiments, in the second case, LDA [12] and incremental LDA (ILDA) [7] were used for feature extraction and SVMs were used for classification. Here also, performance of ILDA +  $2\nu$ -OGSSVM was compared with their batch mode counterpart. Finally, in the third case, modified C2 features were classified using the three classifiers separately. The ROC plots in Figs. 6 - 8, and Tables 2 - 4 show the experimental results for comparison. The key results and analysis are summarized below:

- Baseline PCA (batch/offline learning mode) and IPCA (online learning mode) provide similar verification performance, but the advantage of IPCA is reduced computational cost<sup>3</sup> (Table 5). Specifically, the training time of IPCA is significantly lower compared to PCA. Experimentally, this shows that the online learning approach is a faster alternative for biometrics applications.
- PCA with SVM classifier yields the verification accuracy of 62.23% whereas with  $2\nu$ -GSSVM, the verification accuracy improves by 8.9%. This suggests that incorporating granular computing and soft labels improve the classification performance. Granular computing makes it adaptive to variations in data distribution and soft labels provide resilience to noise.
- If the feature extraction algorithm and classification algorithm are in online learning mode, i.e. IPCA +  $2\nu$ -OGSSVM, verification accuracy is about .1% greater than when both the algorithms are in batch learning mode (PCA +  $2\nu$ -GSSVM). However, the training time in online learning mode, as shown in Table 5 is about half of the batch learning mode which shows the

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<sup>2</sup> In this case study, we observed that  $\gamma = 6$  provided the best verification accuracy for all variations of SVM across all cross validations.

<sup>3</sup> Time was computed on a 2 GHz Pentium Duo Core processor with 2 GB RAM under MATLAB environment.

- suitability of online learning algorithms for large scale real time applications.
- Similar to PCA experiments, LDA experiments also show advantages of online learning (Tables 3 and 5). Here the important point is that in our case study on NIR face verification, accuracies in LDA experiments are better than PCA experiments. This strengthens existing analysis that, in general, LDA yields better accuracy than PCA.
  - Similarly, improvements are observed in the case of modified C2 feature algorithm also. Since the modified C2 algorithm [13] originally uses SVM for classification and decision making, the comparative study is performed with different variants of SVM. Compared to the SVM classifier,  $2\nu$ -OGSSVM not only improves the verification accuracy by 5.77% but also reduces training time by three times.
  - From Tables 2, 3 and 4, the covariate analysis with respect to variations in expression, illumination and pose show that the pose variations cause a large reduction in the accuracy of appearance based PCA and LDA algorithms. On the other hand, local texture feature based modified C2 algorithm provides consistent performance for all three variations. The experiments also show that the modified C2 algorithm with  $2\nu$ -OGSSVM classifier yields the verification accuracy of more than 92% which is around 21.7% better than PCA with  $2\nu$ -OGSSVM classifier and 13.4% better than LDA with  $2\nu$ -OGSSVM classifier.
  - For the three feature extraction algorithms (PCA, LDA and modified C2 feature algorithms), verification accuracies of the proposed  $2\nu$ -OGSSVM are slightly better than  $2\nu$ -GSSVM classifier. However, advantage of  $2\nu$ -OGSSVM is significant reduction in computational time. Compared to classical SVM,  $2\nu$ -GSSVM reduces the training time significantly because the dual- $\nu$  formulation requires less time for parameter estimation and the granular computing approach reduces the time by dividing the problem into sub-problems and solving it efficiently both in terms of accuracy and time. With online learning approach (i.e.  $2\nu$ -OGSSVM), the training time is further reduced because initial training with 100 subjects requires limited computational time (for instance, only 36.1 minutes are required in the case of PCA) and then a relatively small amount of time (22.3 minutes in the case of PCA) is required to train the remaining 228 subjects in online mode (thus the total training time for PCA +  $2\nu$ -OGSSVM is 58.4 minutes). Furthermore, we observed that the computational time required for each update in online mode is small (around 6 seconds). On the other hand, batch mode/offline algorithms have to be retrained using both old and new training data which increases computation cost.
  - From Table 5, even though the PCA, LDA, and modified C2 feature extractors are not trained in online mode, only the online re-training of the classifier improves performance considerably. When the feature extractors are also trained in online mode, i.e. IPCA +  $2\nu$ -OGSSVM and ILDA +  $2\nu$ -OGSSVM, computational time is further decreased.
  - Table 5 also shows that the testing time is considerably reduced when  $2\nu$ -

OGSSVM is used as the classifier. The reason for this improved performance is same as for the reduced training time.

- As mentioned in Section 2, another possible advantage of online learning is to efficiently solve the offline training process in an online manner. To evaluate the appropriateness of this statement in biometric classifier training, a comparative analysis of verification accuracies obtained from  $2\nu$ -GSSVM and  $2\nu$ -OGSSVM is performed. Fig. 9 shows that at the end of learning process with 328 subjects, verification accuracies obtained in the online learning mode is similar to the accuracy obtained in the batch learning mode. Further, the time required for online learning is around half of the offline/batch training. Therefore, it is possible to apply online learning scheme in preference to offline training scheme without affecting the verification accuracy.
- In our experiments, we analyzed the effect of number of support vectors on the verification accuracy across different cross validations. For this case study, at 0.01% FAR, we observed that the number of support vectors in classical SVM batch mode learning was around 1.6 times greater than  $2\nu$ -GSSVM and around 2.3 times greater than  $2\nu$ -OGSSVM. Specifically, across different cross validation trials, average number of support vectors in (1) PCA +  $2\nu$ -OGSSVM case study is 316, (2) LDA +  $2\nu$ -OGSSVM case study is 292 and (3) C2 +  $2\nu$ -OGSSVM case study is 327.
- We performed another experiment in which performance of the proposed  $2\nu$ -OGSSVM algorithm was compared with existing online SVMs namely incremental-decremental SVM [1] and relaxed online SVM [8]. For this comparison we use IPCA and ILDA as online feature extraction algorithms. Under same experimental protocol, Table 6 illustrates the results that clearly show that the proposed algorithm outperforms existing algorithm by at least 4.7%. Also, we observe that the proposed algorithm is around 1.3 times faster than existing algorithms. We observed that this improvement is mainly due to the granularity and soft labels in the proposed  $2\nu$ -OGSSVM classifier.
- At 95% confidence, t-test shows that the  $2\nu$ -GSSVM is significantly different than the SVM classifier whereas there is no statistical difference between  $2\nu$ -GSSVM and  $2\nu$ -OGSSVM. However, as mentioned previously, the main advantage of  $2\nu$ -OGSSVM is reduced computational time and online classifier update.

The experiments demonstrate that online learning approach reduces the computational cost without compromising the verification accuracy. Therefore, it is an effective alternative to traditional batch/offline learning methods.

Table 2

Covariate analysis of PCA and IPCA based verification algorithms with multiple classifiers. Verification accuracies are computed at 0.01% FAR.

Feature Extraction and Classification	Covariate			
	Expression	Illumination	Pose	Overall
PCA [11]	51.87	52.24	45.46	49.21
PCA + SVM	64.76	65.34	58.17	62.23
PCA + $2\nu$ -SVM	64.98	65.83	58.41	62.95
PCA + $2\nu$ -GSSVM	73.63	74.04	67.86	71.14
PCA + $2\nu$ -OGSSVM	72.82	73.95	67.49	70.97
IPCA [6]	51.73	52.21	45.02	49.17
IPCA + $2\nu$ -OGSSVM	<b>73.67</b>	<b>74.11</b>	<b>67.92</b>	<b>71.22</b>

Table 3

Covariate analysis of LDA and ILDA based verification algorithms with multiple classifiers. Verification accuracies are computed at 0.01% FAR.

Feature Extraction and Classification	Covariate			
	Expression	Illumination	Pose	Overall
LDA [12]	62.01	62.43	54.97	60.82
LDA + SVM	70.84	71.28	58.61	69.01
LDA + $2\nu$ -SVM	70.97	71.58	59.08	73.85
LDA + $2\nu$ -GSSVM	80.75	81.13	71.06	79.04
LDA + $2\nu$ -OGSSVM	80.71	81.15	70.81	78.99
ILDA [7]	61.82	62.19	54.13	60.76
ILDA + $2\nu$ -OGSSVM	<b>80.83</b>	<b>81.20</b>	<b>70.98</b>	<b>79.35</b>

Table 4

Covariate analysis of modified C2 based verification algorithm with multiple classifiers. Verification accuracies are computed at 0.01% FAR.

Feature Extraction and Classification	Covariate			
	Expression	Illumination	Pose	Overall
C2 + SVM	87.76	87.93	85.17	86.94
C2 + $2\nu$ -SVM	87.79	88.02	85.59	87.21
C2 + $2\nu$ -GSSVM	92.67	92.85	91.81	92.46
C2 + $2\nu$ -OGSSVM	<b>92.79</b>	<b>92.88</b>	<b>92.03</b>	<b>92.71</b>

Table 5

Computational time analysis for the proposed  $2\nu$ -OGSSVM and comparison with other classification approaches.

Feature Extraction + Classification	Computation Time	
	Training Time (Minutes)	Testing Time (Seconds)
PCA [11]	43.6	0.5
PCA + SVM	221.5	1.7
PCA + $2\nu$ -SVM	194.8	1.4
PCA + $2\nu$ -GSSVM	118.2	1.1
PCA + $2\nu$ -OGSSVM	58.4	0.8
IPCA [6]	31.2	0.4
IPCA + $2\nu$ -OGSSVM	<b>52.5</b>	<b>0.7</b>
LDA [12]	48.8	0.6
LDA + SVM	230.1	1.8
LDA + $2\nu$ -SVM	198.4	1.6
LDA + $2\nu$ -GSSVM	122.6	1.2
LDA + $2\nu$ -OGSSVM	61.9	0.9
ILDA [7]	37.2	0.5
ILDA + $2\nu$ -OGSSVM	<b>55.1</b>	<b>0.8</b>
C2 + SVM	336.8	2.1
C2 + $2\nu$ -SVM	282.1	1.8
C2 + $2\nu$ -GSSVM	192.4	1.6
C2 + $2\nu$ -OGSSVM	<b>109.7</b>	<b>1.2</b>

Table 6

Comparison of  $2\nu$ -OGSSVM with existing online SVMs. Verification accuracies are computed at 0.01% FAR.

Feature Extraction Algorithm	Online Classifier		
	Relaxed Online SVM [8]	Incremental-decremental SVM [1]	Proposed $2\nu$ -OGSSVM
IPCA	65.81	66.53	<b>71.22</b>
ILDA	71.48	71.97	<b>79.35</b>



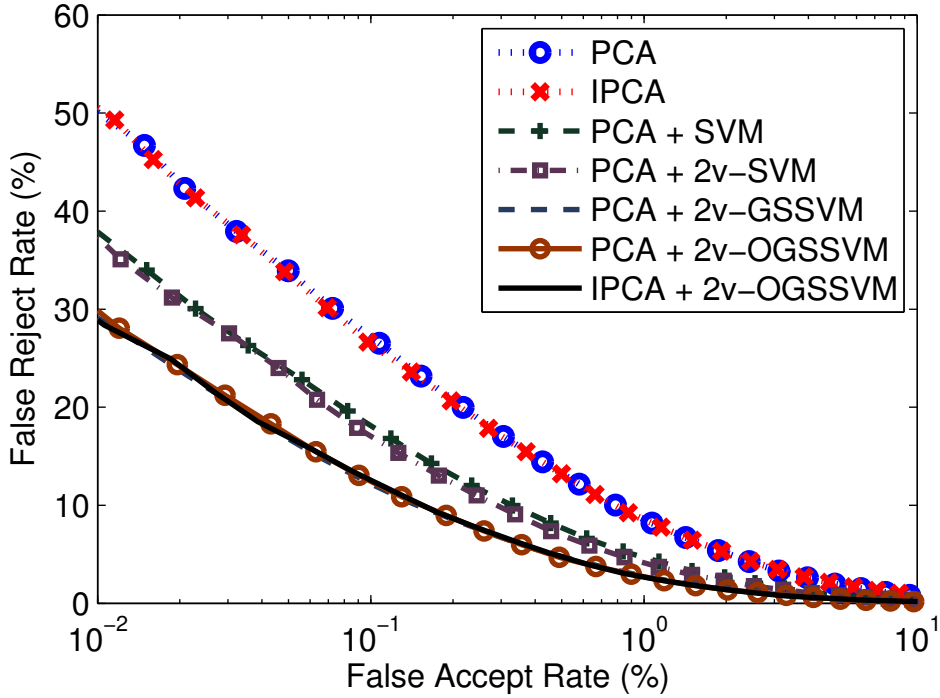


Fig. 6. Comparing the performance of the proposed  $2\nu$ -OGSSVM (online classifier) with SVM and  $2\nu$ -GSSVM using appearance based PCA/IPCA algorithm.

### 5 Conclusion and Future Work

Similar to template update, the parameters of the classifiers used in biometric system also require to be updated to accommodate for variations in data distribution. Current systems frequently re-train the algorithms using all enrolled subjects. This process may not be feasible for large scale systems where the number of newly enrolled subjects is significantly high. This paper introduces the concept of online learning in biometrics to address the problem of classifier re-training and update. An online learning scheme for  $2\nu$ -GSSVM is proposed to train the classifier in online mode so that it can update the decision hyper-plane according to the newly enrolled subjects. This online classifier is used for feature classification and decision making in a face verification system. On a heterogeneous NIR face database, the case study using PCA, LDA and modified C2 feature algorithms shows that the proposed online classifier significantly improves the verification performance both in terms of accuracy and computational time. Indeed, it is observed that the proposed online classifier is at least three times faster than the conventional SVM classifier.

The emergence and viability of using online learning algorithms in the design of biometric classifiers addresses the real-time performance and scalability challenges, however more research is required in order to fully understand the benefits in large-scale applications. It is our assertion that the promising

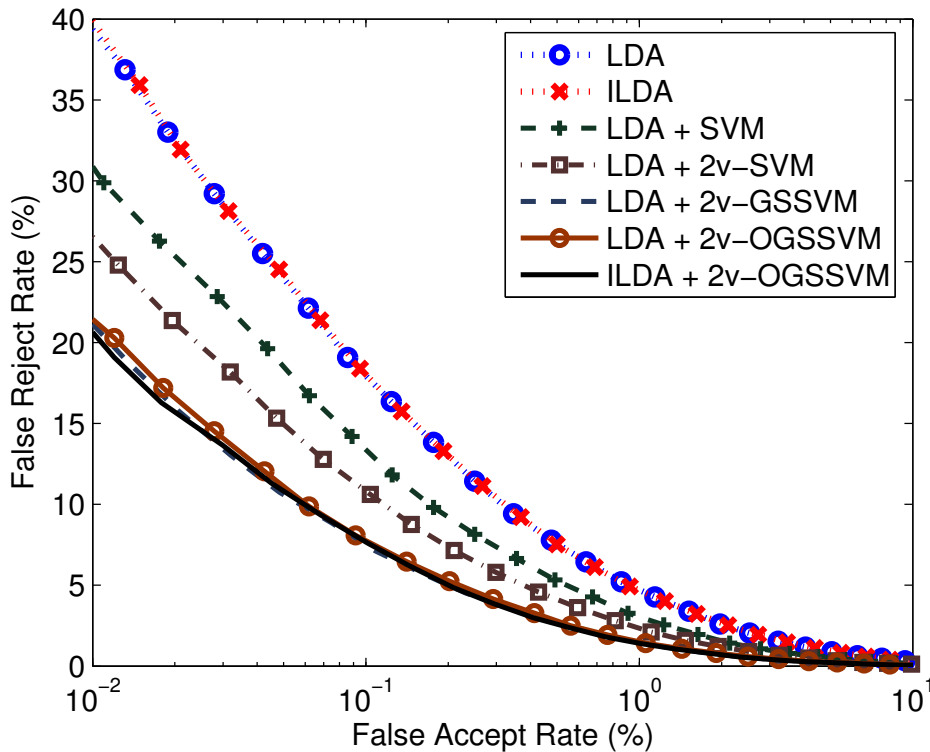


Fig. 7. Comparing the performance of the proposed  $2\nu$ -OGSSVM (online classifier) with SVM and  $2\nu$ -GSSVM using appearance based LDA/ILDA algorithm.

research results of this work would stimulate further research in this important area. Currently, we are investigating possibilities of applying online learning concept at feature level and biometrics template update.

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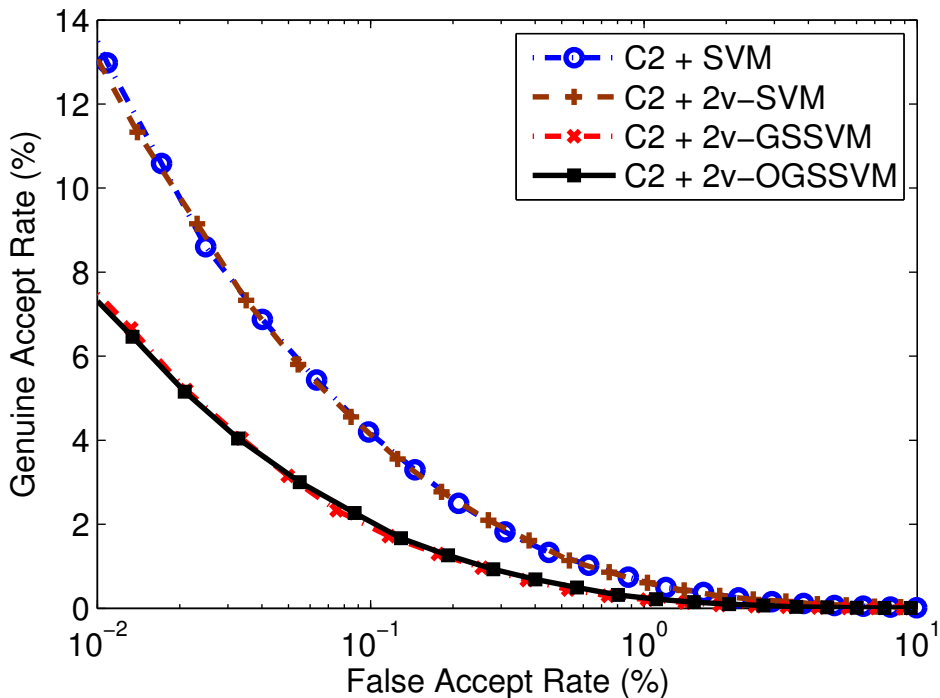
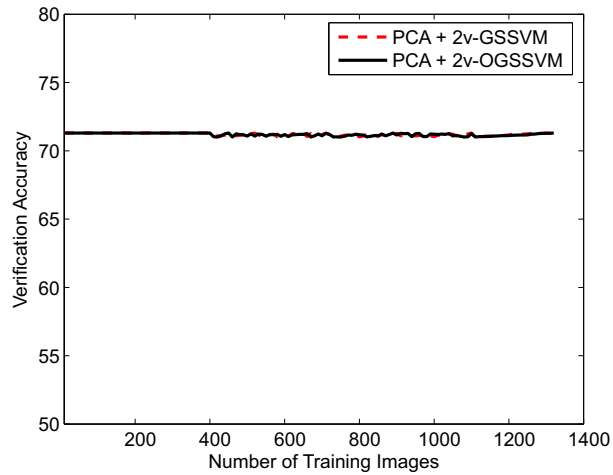


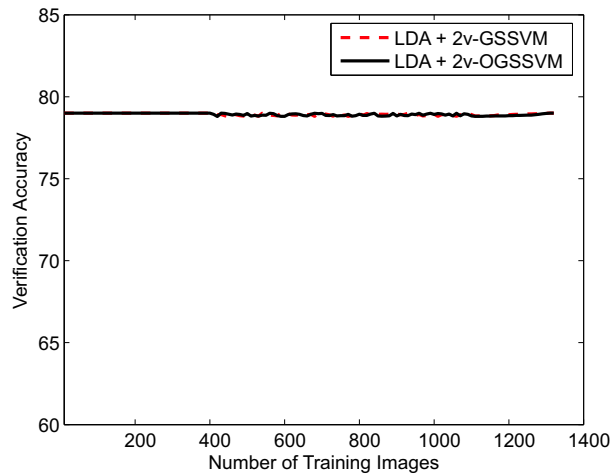
Fig. 8. Comparing the performance of the proposed  $2\nu$ -OGSSVM (online classifier) with SVM and  $2\nu$ -GSSVM using local texture feature based modified C2 algorithm [13].

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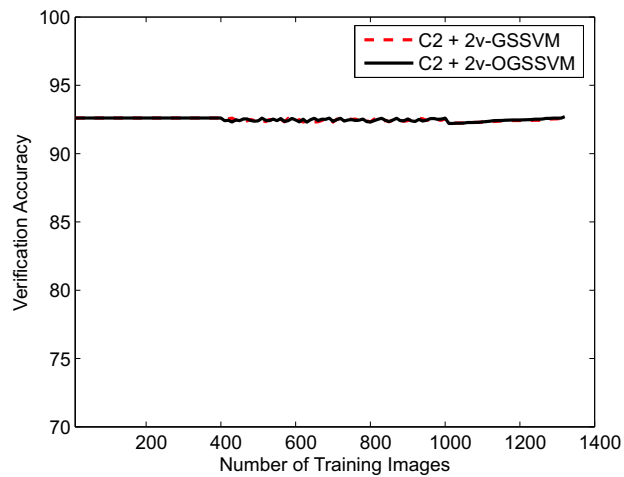
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(a)



(b)



(c)

Fig. 9. Verification accuracy when adding new training samples (i.e. new classes and new class instances): (a) PCA (b) LDA and (c) modified C2 algorithms. Note that x-axis represents 1312 training images pertaining to 328 subjects and first 400 images pertaining to 100 subjects are initial training images.

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